

THIRD TERM E-LEARNING NOTE

SUBJECT: MATHEMATICS

CLASS: SS2

SCHEME OF WORK

WEEK	TOPIC
1	Circle Theorem: Tangent properties of circle; Angles in alternate segment; Two tangent from a circle at external point.
2	Trigonometry: Derivative of sine rule and cosine rule and their applications.
3	Bearing and Distances; Elevation and Depression.
4	Statistics: Class boundaries, class mark, and cumulative frequencies of grouped data, and histogram.
5	Statistics: Cumulative frequency curve (Ogive); Using ogive to calculate the median, quartile, percentile and decile.
6	Review of the First Half Term Work and Periodic Test.
7	Statistics: Mean, median, and mode of grouped data.
8	Probability: Introduction; use of dice, coins and playing cards.
9	Probability: Addition and multiplication rules of probability; Mutually exclusive, independent, and complementary events; Experiment with or without replacement.
10	Revision

REFERENCE BOOKS

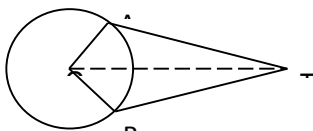
1. New General Mathematics SSS2 by M.F. Macrae et al.
2. Essential Mathematics SSS2 by A.J.S. Oluwasanmi.
3. Exam Focus Mathematics.

WEEK ONE

TOPIC: TANGENTS FROM AN EXTERNAL POINT

Theorem:

The tangents to a circle from an external point are equal.



Given: a point T outside a circle, centre O, TA and TB are tangents to the circle at A and B.

To prove: $|TA| = |TB|$

Construction: Join OA, OB and OT

In Δ s OAT and OBT

$\angle OAT = \angle OBT = 90^\circ$ (radius \perp tangent)

$|OA| = |OB|$ (radii)

$|OT| = |OT|$ (common side)

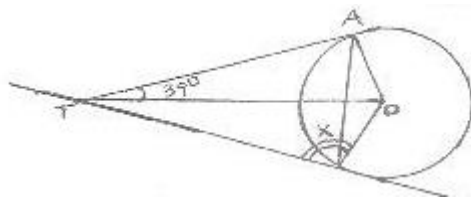
$\Delta OAT = \Delta OBT$ (RHS)

$|TA| = |TB|$

Note that $\angle AOT = \angle BOT$ and $\angle ATO = \angle BTO$ hence the line joining the external point to the centre of the circle bisects the angle between the tangents and the angle between the radii drawn to the points of contact of the tangents.

Example:

1. In the figure below O is the centre of the circle and the TA and TB are tangents if $\angle ATO = 39^\circ$, calculate $\angle TBX$



In ΔTAX

$\angle AXT = 90^\circ$ (Symmetry)

$\angle TAX = 180^\circ - (90^\circ + 39^\circ)$ (sum of angles of Δ)

$180^\circ - 129^\circ = 51^\circ$

$\angle TBX = 51^\circ$ (symmetry)

OR

ΔATB is an Isosceles triangle

$|AT| = |BT|$ (tangents from external point)

$\angle ATO = \angle BTO = 39^\circ$ (symmetry)

$\angle ATB = 2(39) = 78^\circ$

$\angle TAX = \angle TBX$ (base angle of Isos Δ)

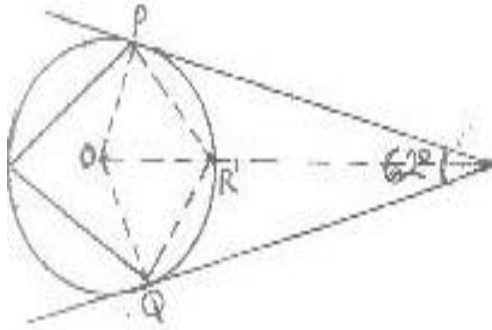
$2\angle TBX = 180^\circ - 78^\circ$ (sum of angle in a Δ)

$2\angle TBX = 102^\circ$

$$\angle TBX = \frac{102^\circ}{2}$$

$\angle TBX = 51^\circ$

2. PQR are three points on a circle Centre O. The tangent at P and Q meet at T. If $\angle PTQ = 62^\circ$ calculate $\angle PRQ$.



Solution

Join OP and OQ

In quadrilateral TQOP

$\angle OQT = \angle OPT = 90^\circ$ (radius \perp tangent)

$\angle POQ = 360^\circ - (90^\circ + 90^\circ + 62^\circ)$ (sum of angle in a quadrilateral)

$\angle POQ = 360^\circ - 242^\circ$

$\angle POQ = 118^\circ$

$\angle PRQ = \frac{118^\circ}{2} = 59^\circ$ (2x angle at circumference = angle at centre)

PR¹QR is a cyclic quadrilateral

$R + R^1 = 180^\circ$ (opp. angles of a cyclic quadrilateral)

$R^1 = 180^\circ - R$

$R^1 = 180^\circ - 59^\circ$

$R^1 = 121^\circ$

$\angle PRQ = 59^\circ$ or 121°

Evaluation

1. ABC are three points on a ...